

Deep Scatter Estimation (DSE): Feasibility of using a Deep Convolutional Neural Network for Real-Time X-Ray Scatter Prediction in Cone-Beam CT

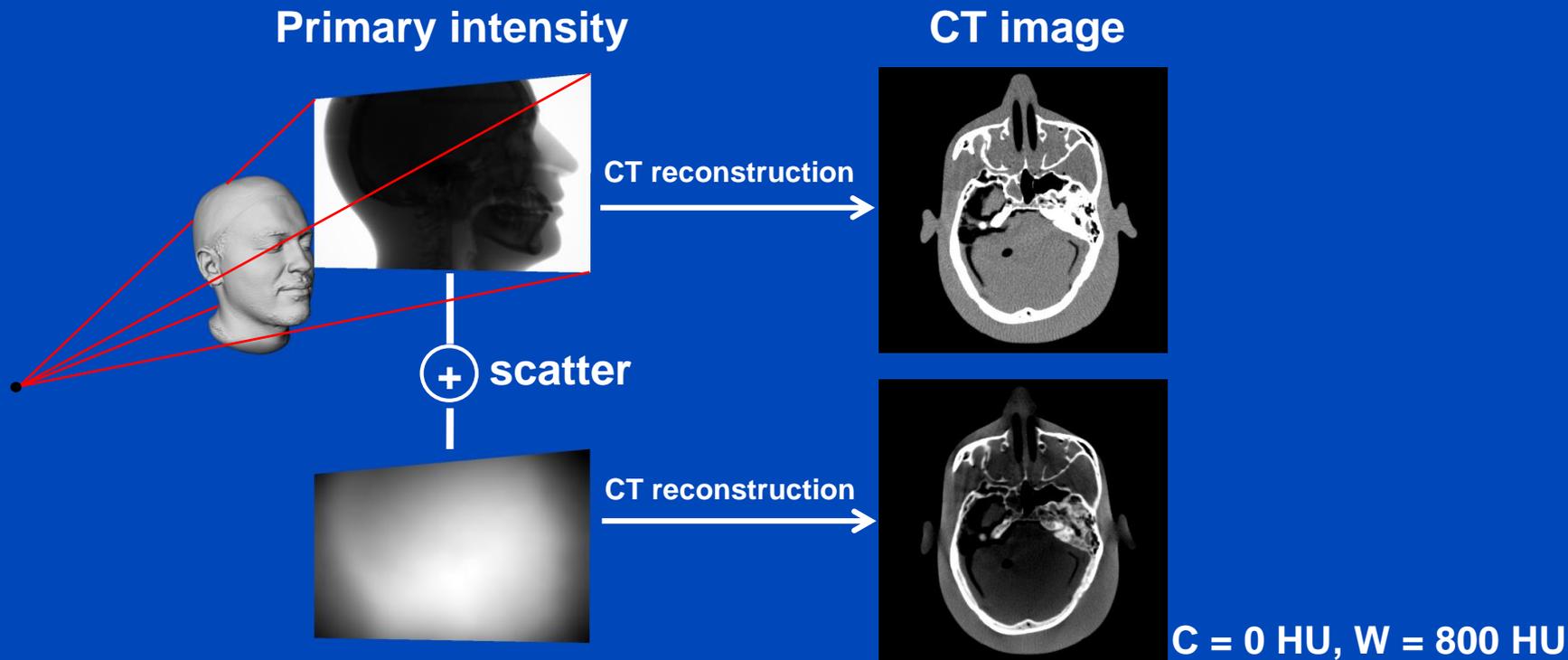
Joscha Maier^{1,2}, Yannick Berker¹, Stefan Sawall^{1,2}
and Marc Kachelrieß^{1,2}

¹German Cancer Research Center (DKFZ), Heidelberg, Germany

²Ruprecht-Karls-Universität, Heidelberg, Germany

Motivation

- X-ray scatter is a major cause of image quality degradation in CT and CBCT.
- Appropriate scatter correction is crucial to maintain the diagnostic value of the CT examination.



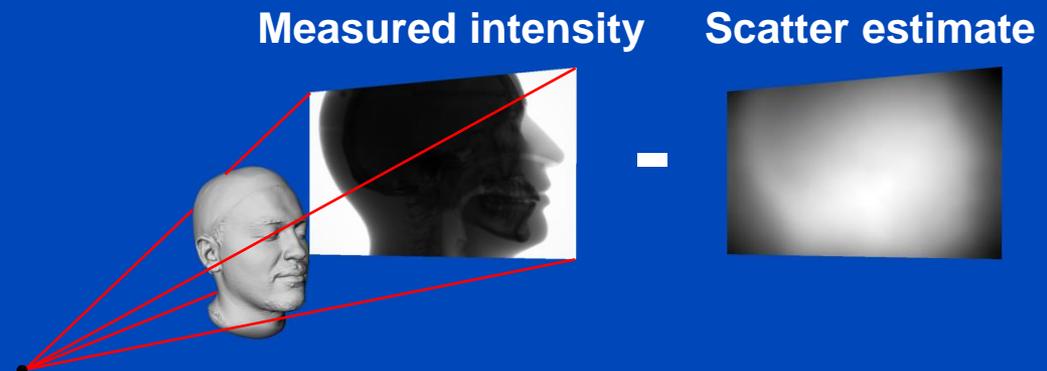
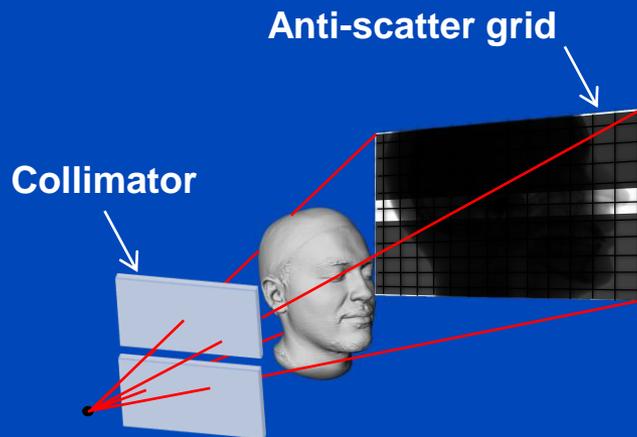
Scatter Correction

Scatter suppression

- Anti-scatter grids
- Collimators
- ...

Scatter estimation

- Monte Carlo simulation
- Kernel-based approaches
- Boltzmann transport
- Primary modulation
- Beam blockers
- ...

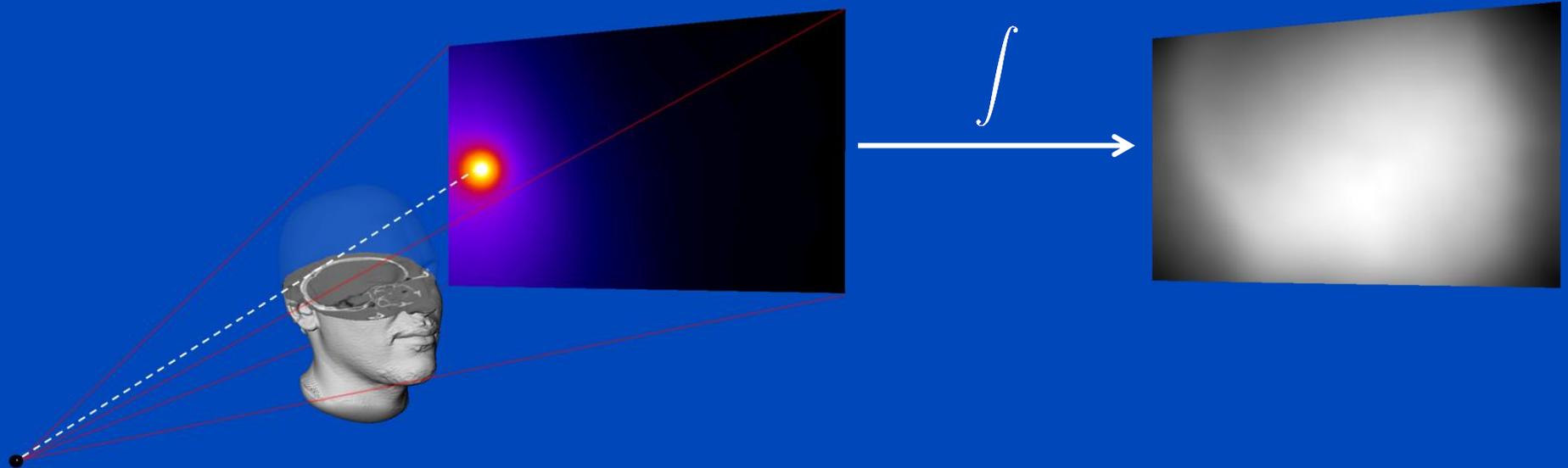


Monte Carlo Scatter Estimation

- Simulation of photon trajectories according to physical interaction probabilities.
- Simulating a large number of photon trajectories well approximates the expectation value of the actual scatter distribution.

Scatter distribution of an incident needle beam

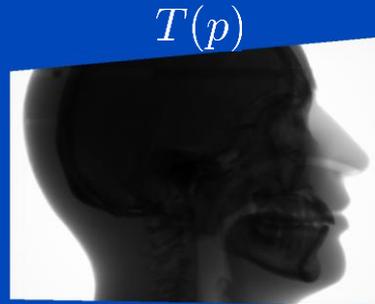
Complete scatter distribution



Kernel-Based Scatter Estimation

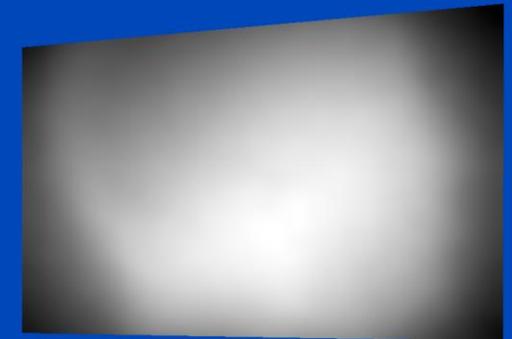
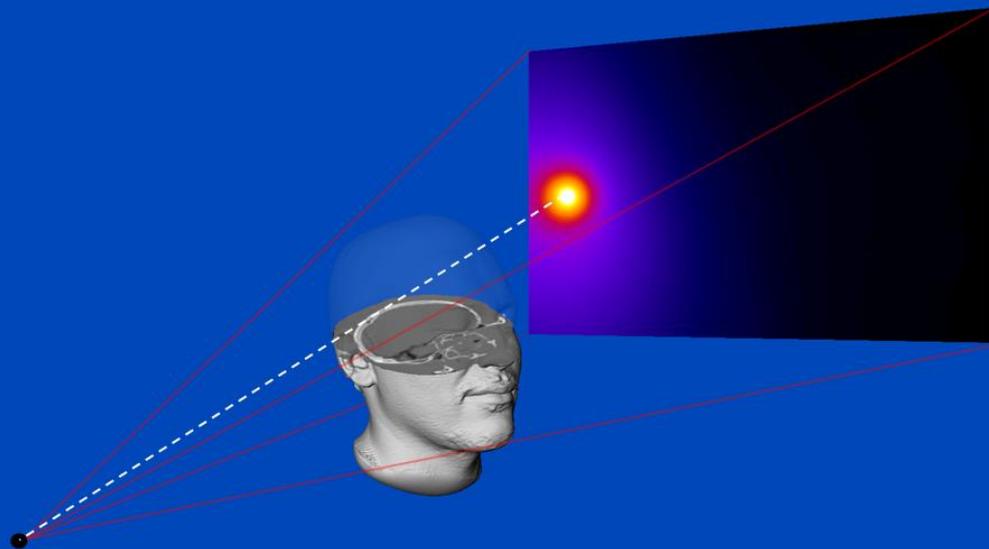
Estimate needle beam scatter kernels as a function of the projection data p

$$I_{s, \text{est}}(\mathbf{u}) = \int T(p)(\mathbf{u}') G(\mathbf{u}, \mathbf{u}', \mathbf{c}) d\mathbf{u}'$$



Estimate mean scatter kernel that maps a function of the projection data p to scatter distribution

$$I_{s, \text{est}}(\mathbf{u}) = T(p)(\mathbf{u}) * G(\mathbf{u}, \mathbf{c})$$



Deep Scatter Estimation (DSE)

Idea

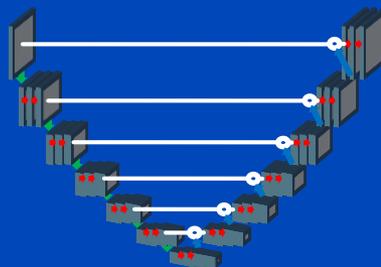
- Train a deep convolutional neural network to estimate scatter using a function of the acquired projection data as input.

Input: $T(p)$

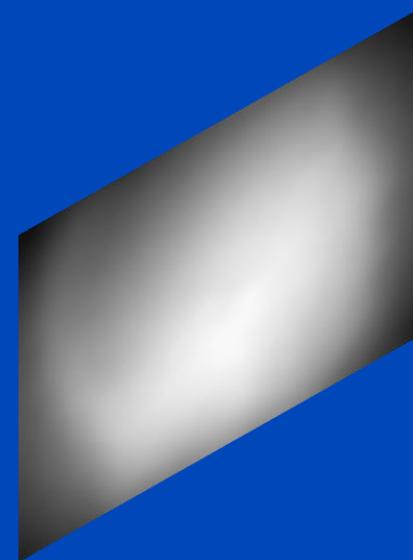


$$\int T(p)(u') G(u, u', c) du'$$

Convolutional neural network



Scatter estimate



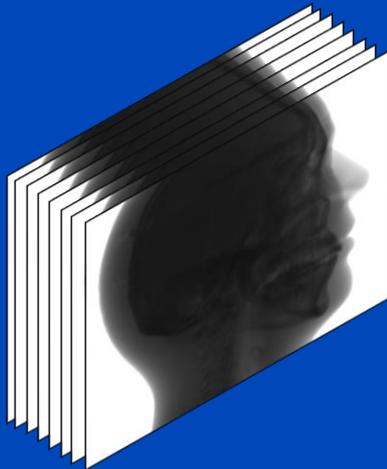
Deep Scatter Estimation (DSE)

Training of the network

- Optimize weights and biases of convolutional network such that the mean squared error between the output and MC scatter simulations is minimal:

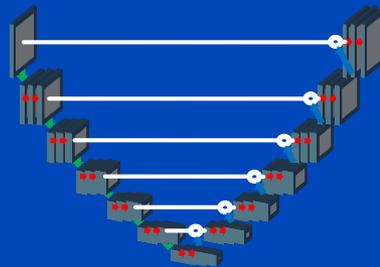
$$\{w, b\} = \operatorname{argmin} \|DSE(T(p)) - I_{MC}\|_2^2$$

Input: $T(p)$

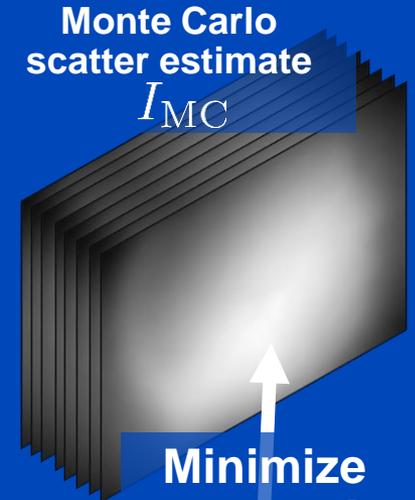


Convolutional neural network

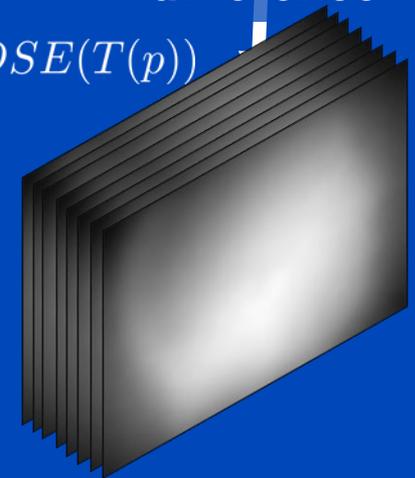
~~$$\int T(p)(u') G(u, u', c) du'$$~~



$DSE(T(p))$

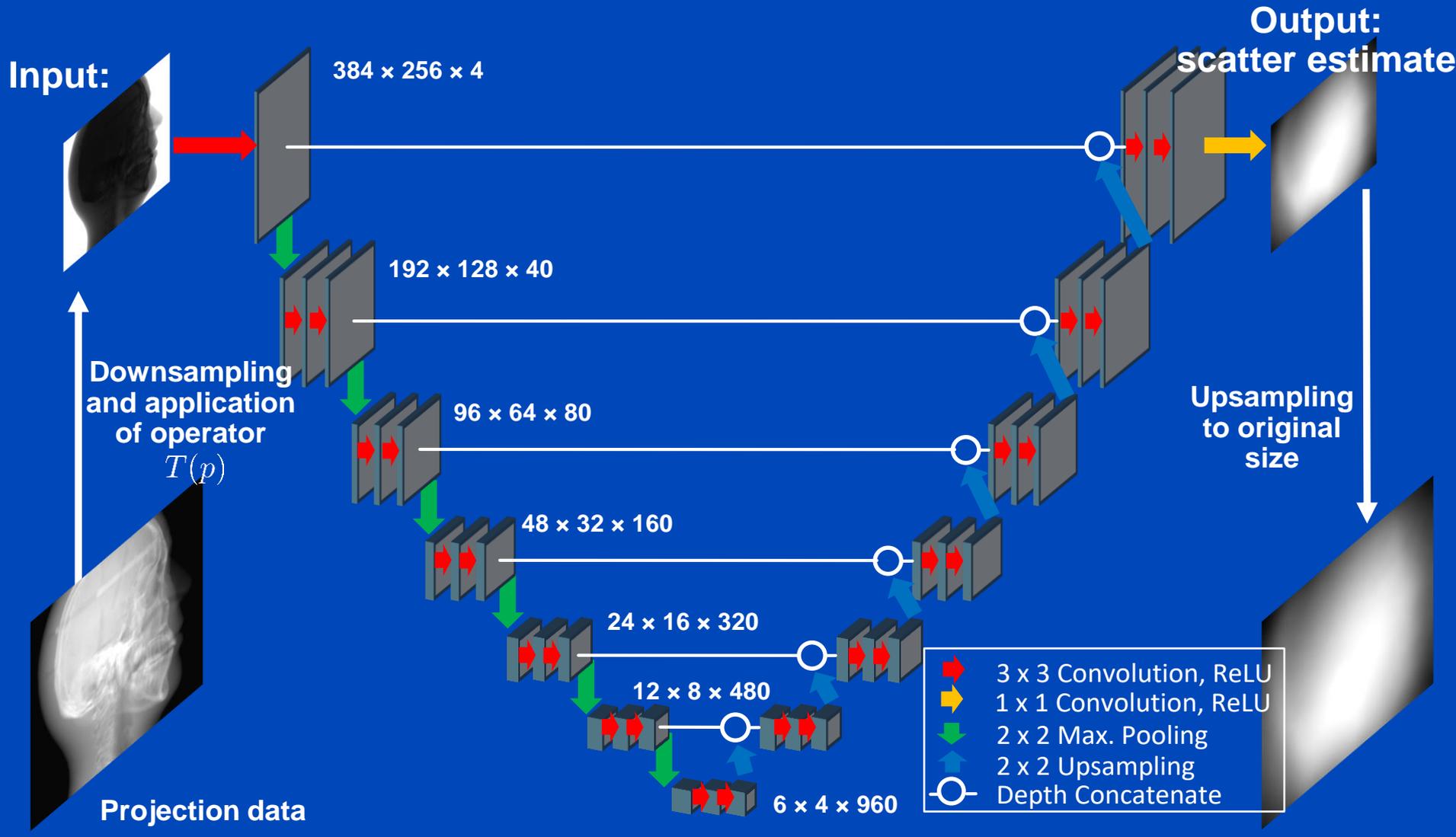


Minimize squared difference



Deep Scatter Estimation

Network architecture & scatter estimation framework



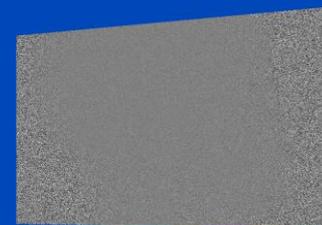
Training of the DSE Network

CBCT Setup

Primary intensity

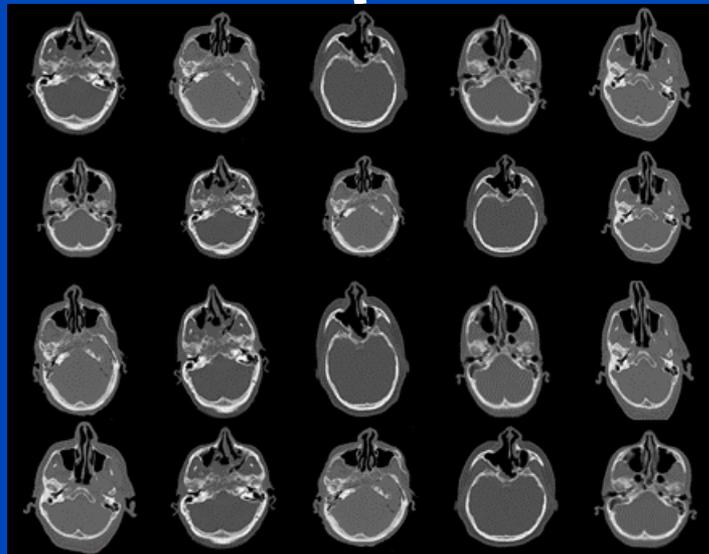
MC scatter simulation

Poisson noise



Input

Desired output



- Simulation of 12000 projection data using simulations of different heads and different acquisition parameters.
- Splitting into 80 % training and 20 % validation data.
- Optimize weights of convolutional network to reproduce Monte Carlo scatter estimates:

$$\{w, b\} = \operatorname{argmin} \|DSE(T(p)) - I_{MC}\|_2^2$$

- Training on a GeForce GTX 1080 for 80 epochs.

Testing of the DSE Network

Simulated Data

CBCT Setup

Primary intensity

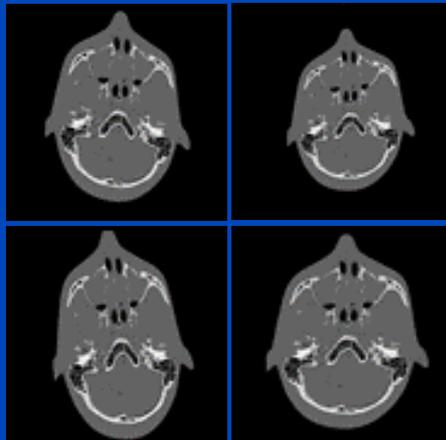
MC scatter simulation

Poisson noise

Input

Ground truth

- Application of the DSE network to predict scatter for simulated data of a head (different from training data).



Testing of the DSE Network

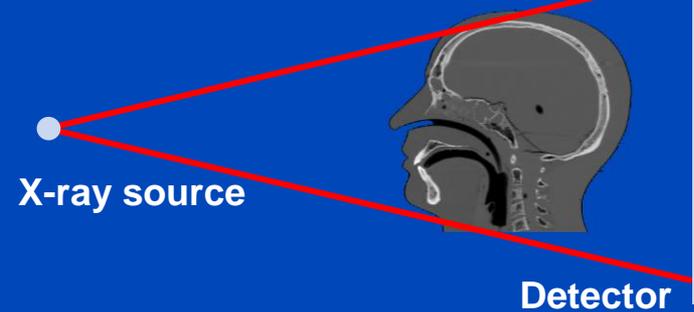
Measured Data

DKFZ table-top CT

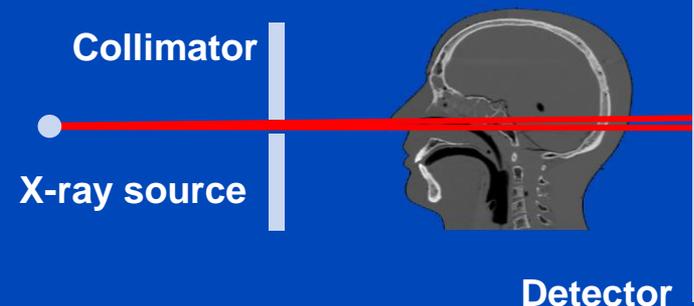


- Measurement of a head phantom at our in-house table-top CT.
- Slit scan measurement serves as ground truth.

Measurement to be corrected



Ground truth: slit scan



Reference 1

Kernel-based scatter estimation

- Kernel-based scatter estimation¹:

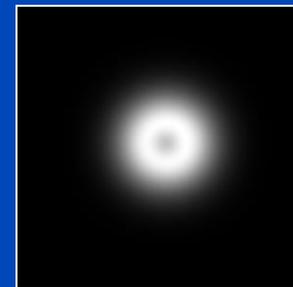
- Estimation of scatter by a convolution of the scatter source term $T(p)$ with a scatter propagation kernel $G(u, c)$:

$$I_{s, \text{ est}}(\mathbf{u}) = \underbrace{\left(c_0 \cdot p(\mathbf{u}) \cdot e^{-p(\mathbf{u})} \right)}_{T(p)(\mathbf{u})} * \underbrace{\left(\sum_{\pm} e^{-c_1(u\hat{e}_1 \pm c_2)^2} \cdot \sum_{\pm} e^{-c_3(u\hat{e}_2 \pm c_4)^2} \right)}_{G(\mathbf{u}, \mathbf{c})}$$



$T(p)(\mathbf{u})$

Open
parameters:
 c_0



$G(\mathbf{u}, \mathbf{c})$

Open
parameters:
 c_1, c_2, c_3, c_4

$$\{c_i\} = \underset{\{c_i\}}{\operatorname{argmin}} \sum_n \sum_{\mathbf{u}} \|I_{s, \text{ est}}(n, \mathbf{u}, \{c_i\}) - I_s(n, \mathbf{u})\|_2^2,$$

Samples of the
training data set

Scatter estimate

MC scatter simulation

Detector
coordinate



¹ B. Ohnesorge, T. Flohr, K. Klingensbeck-Regn: Efficient object scatter correction algorithm for third and fourth generation CT scanners. Eur. Radiol. 9, 563–569 (1999).

Reference 2

Hybrid scatter estimation

- Hybrid scatter estimation² :

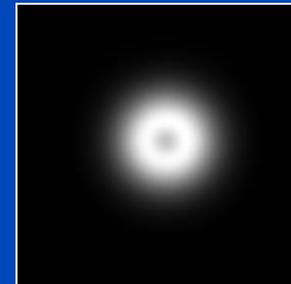
- Estimation of scatter by a convolution of the scatter source term $T(p)$ with a scatter propagation kernel $G(u, c)$:

$$I_{s, \text{ est}}(\mathbf{u}) = \underbrace{\left(c_0 \cdot p(\mathbf{u}) \cdot e^{-p(\mathbf{u})} \right)}_{T(p)(\mathbf{u})} * \underbrace{\left(\sum_{\pm} e^{-c_1(\mathbf{u}\hat{\mathbf{e}}_1 \pm c_2)^2} \cdot \sum_{\pm} e^{-c_3(\mathbf{u}\hat{\mathbf{e}}_2 \pm c_4)^2} \right)}_{G(\mathbf{u}, \mathbf{c})}$$



$T(p)(\mathbf{u})$

Open parameters:
 c_0



$G(\mathbf{u}, \mathbf{c})$

Open parameters:
 c_1, c_2, c_3, c_4

$$\{c_i\}_n = \operatorname{argmin}_{\mathbf{u}} \sum_{\mathbf{u}} \|I_{s, \text{ est}}(n, \mathbf{u}, \{c_i\}) - I_s(n, \mathbf{u})\|_2^2,$$

Samples of the test data set

Detector coordinate

Scatter estimate

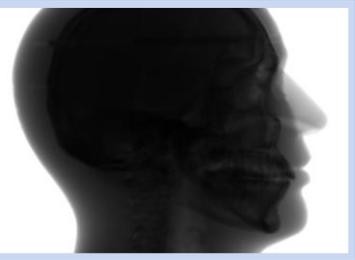


Coarse MC simulation



Performance on Validation Data for Different Inputs

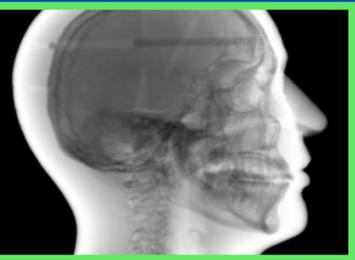
$$T(p) = e^{-p}$$



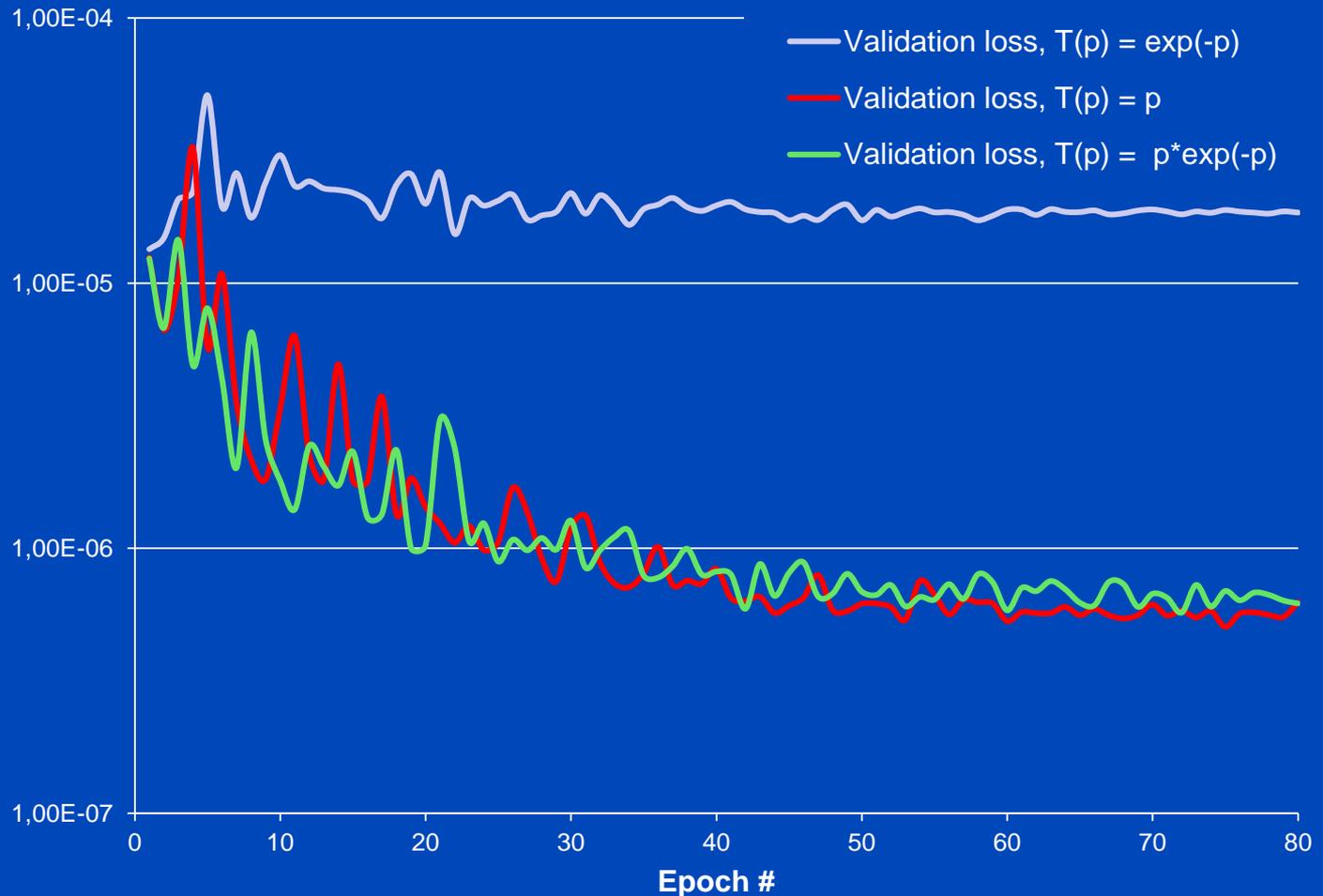
$$T(p) = p$$



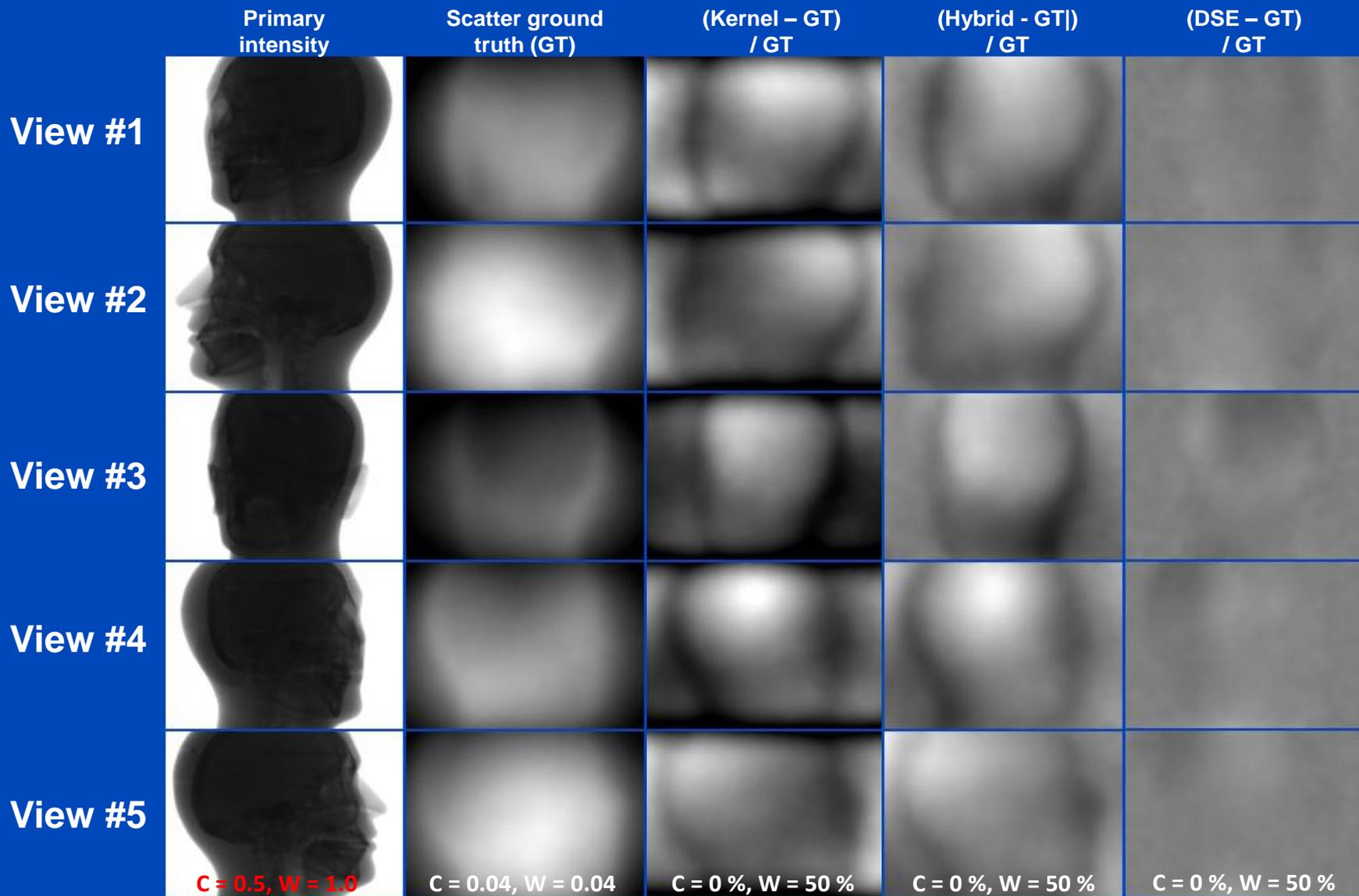
$$T(p) = p \cdot e^{-p}$$



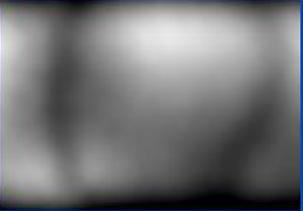
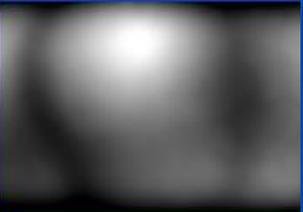
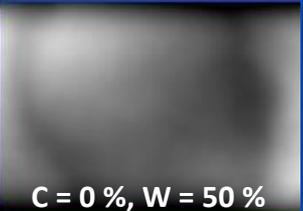
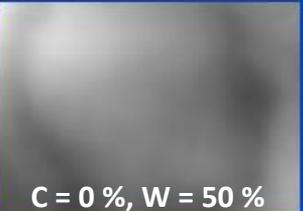
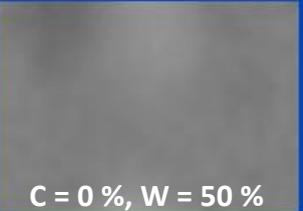
Mean squared error between output and MC simulation



Results – Simulated Projection Data



Results – Simulated Projection Data

	Primary intensity	Scatter ground truth (GT)	(Kernel – GT) / GT	(Hybrid - GT) / GT	(DSE – GT) / GT
View #1					
View #2					
View #3			Mean absolute error for all projections: 14.1 % 7.2 % 1.2 %		
View #4					
View #5					
	C = 0.5, W = 1.0	C = 0.04, W = 0.04	C = 0 %, W = 50 %	C = 0 %, W = 50 %	C = 0 %, W = 50 %

Results – CT Reconstructions of Simulated Data

Ground Truth

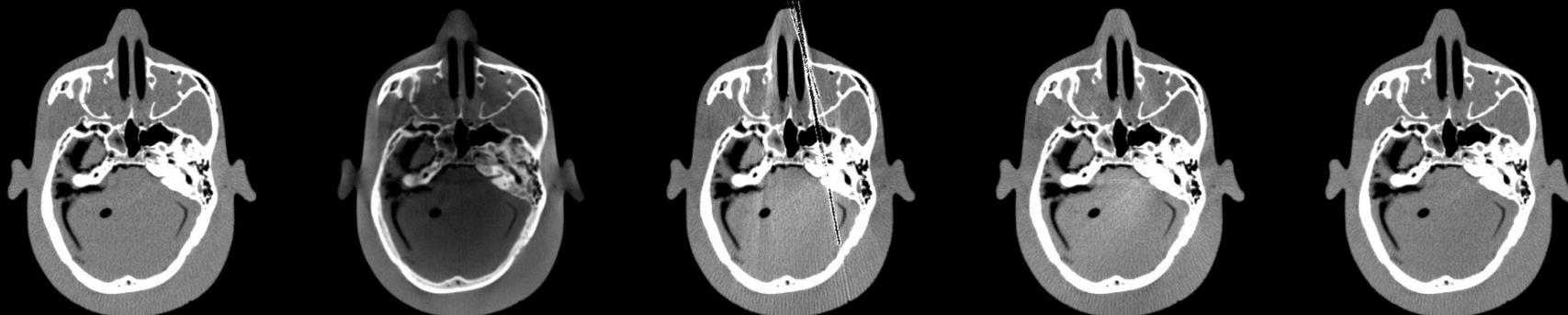
No Correction

Kernel-Based Scatter Estimation

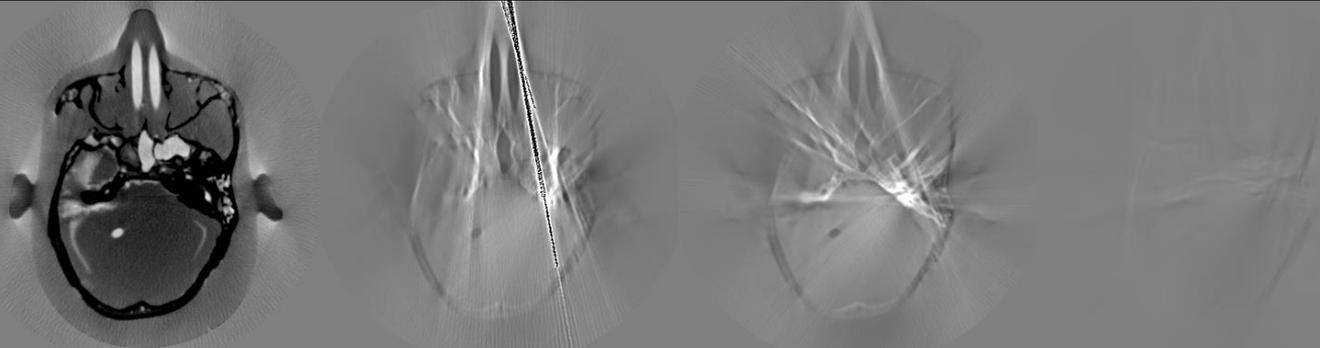
Hybrid Scatter Estimation

Deep Scatter Estimation

CT Reconstruction



Difference to ideal simulation



$C = 0$ HU, $W = 1000$ HU

Results – CT Reconstructions of Measured Data

Slit Scan

No Correction

Kernel-Based Scatter Estimation

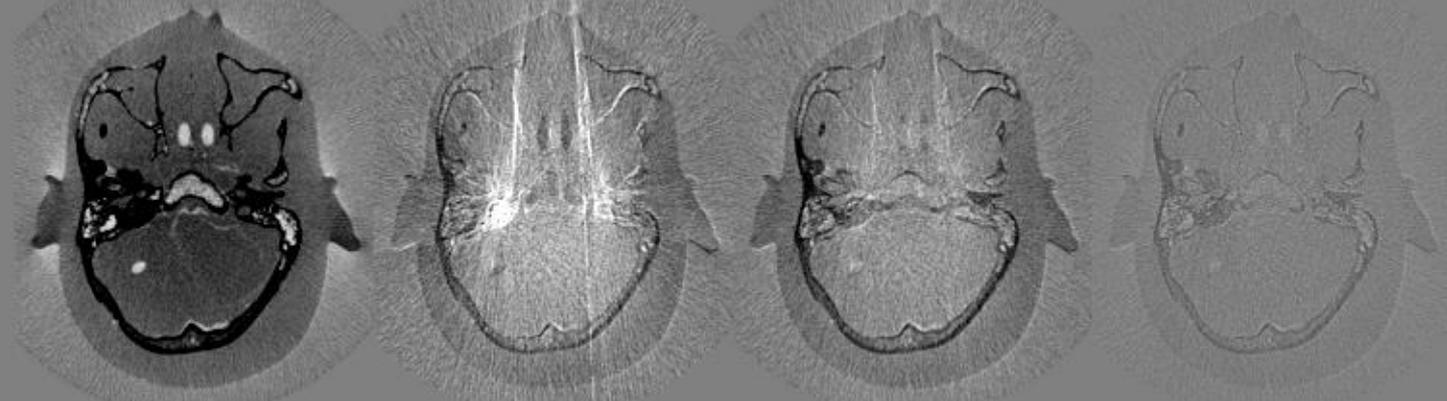
Hybrid Scatter Estimation

Deep Scatter Estimation

CT Reconstruction



Difference to slit scan



$C = 0 \text{ HU}$, $W = 1000 \text{ HU}$

Conclusions

- **DSE is a fast and accurate alternative to Monte Carlo simulation.**
- **DSE outperforms conventional kernel-based approaches in terms of accuracy.**
- **DSE is not restricted to reproduce only Monte Carlo scatter estimates but can be used with any other scatter estimate.**

Thank You!

This presentation will soon be available at www.dkfz.de/ct

Job opportunities through DKFZ's international PhD or Postdoctoral Fellowship programs (www.dkfz.de), or directly through Prof. Dr. Marc Kachelrieß (marc.kachelriess@dkfz.de).

Parts of the reconstruction software were provided by RayConStruct® GmbH, Nürnberg, Germany.