

# Deep Scatter Estimation (DSE) for Truncated Cone-Beam CT (CBCT)

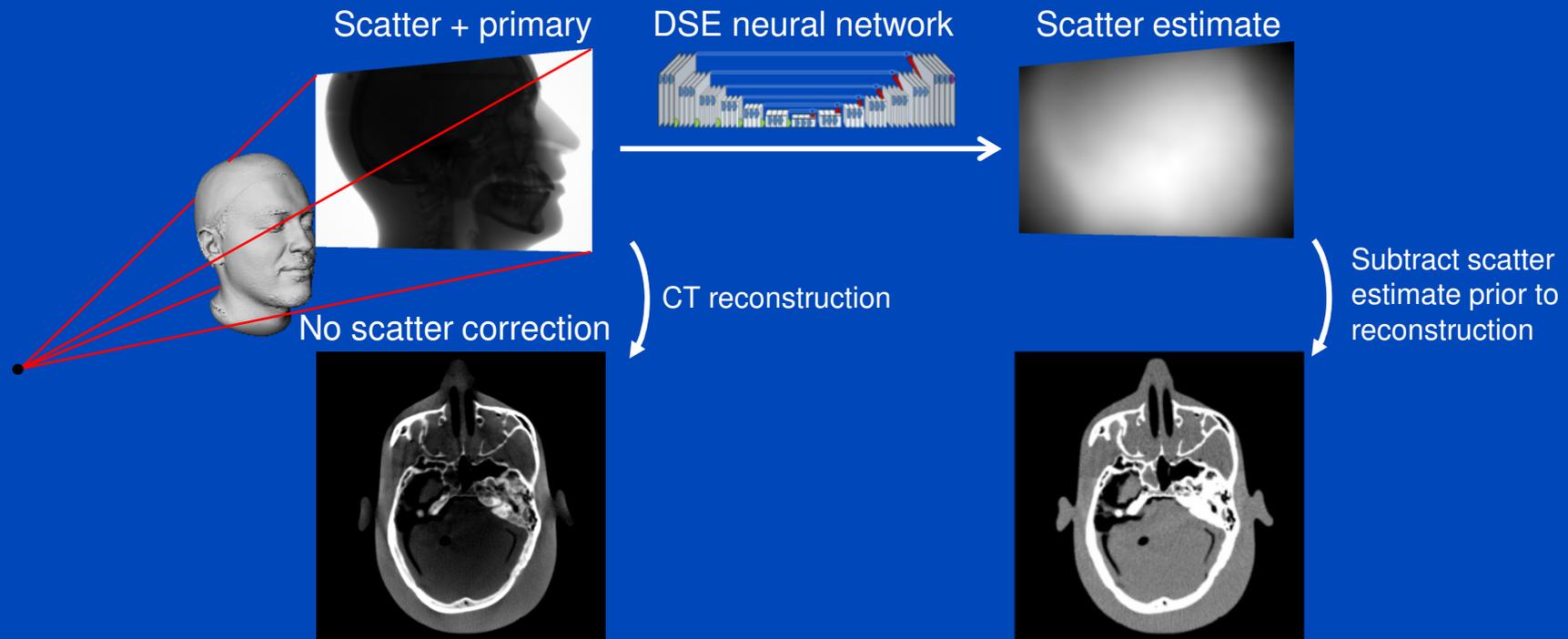
Joscha Maier<sup>1,2</sup>, Elias Eulig<sup>1,2</sup>, Stefan Sawall<sup>1,2</sup>  
and Marc Kachelrieß<sup>1,2</sup>

<sup>1</sup>German Cancer Research Center (DKFZ), Heidelberg, Germany

<sup>2</sup>Ruprecht-Karls-Universität, Heidelberg, Germany

# Motivation

- X-ray scatter leads to a degradation of image quality in CT.
- Appropriate scatter correction is crucial to maintain the diagnostic and quantitative value of the CT examination.
- Recently, we proposed the deep scatter estimation (DSE)<sup>1,2</sup> which has demonstrated great potential for scatter-correction of non-truncated CBCT simulations and measurements.



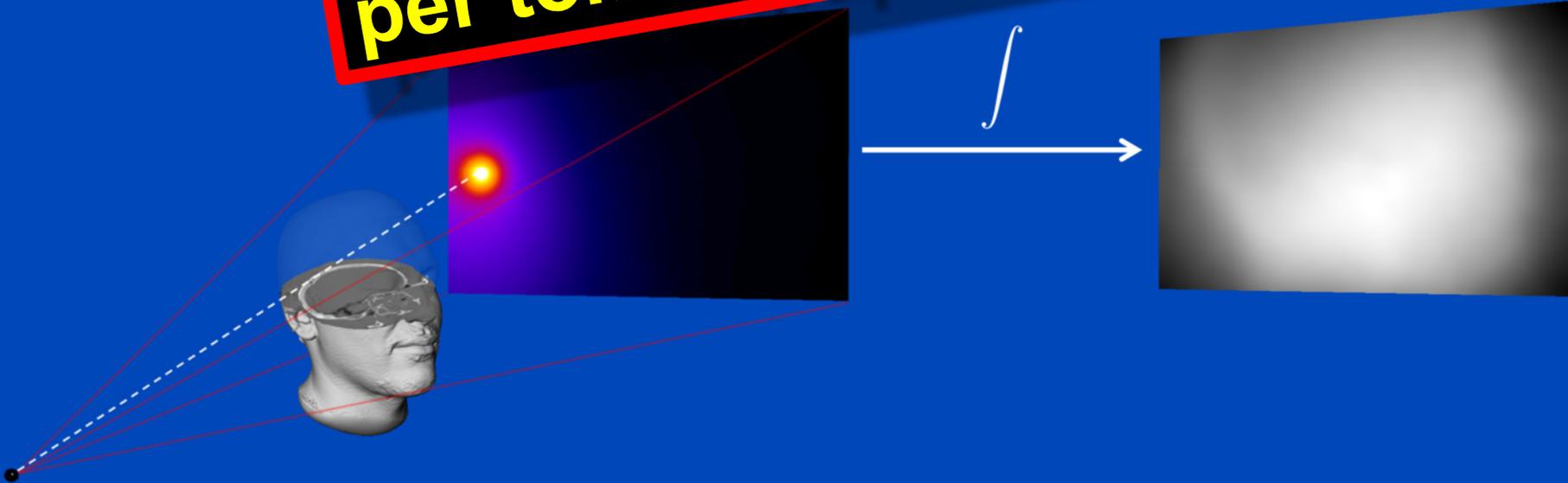
<sup>1</sup>J. Maier, Y. Berker, S. Sawall, M. Kachelrieß. SPIE Medical Imaging Conference Record 105731L:1-6, 2018.

<sup>2</sup>J. Maier, S. Sawall, M. Knaup, M. Kachelrieß. Journal of Nondestructive Evaluation 37:57, 2018.

# Monte Carlo Scatter Estimation

- Simulation of photon trajectories according to physical interaction probabilities.
- Simulating a large number of trajectories well approximates the complete scatter distribution

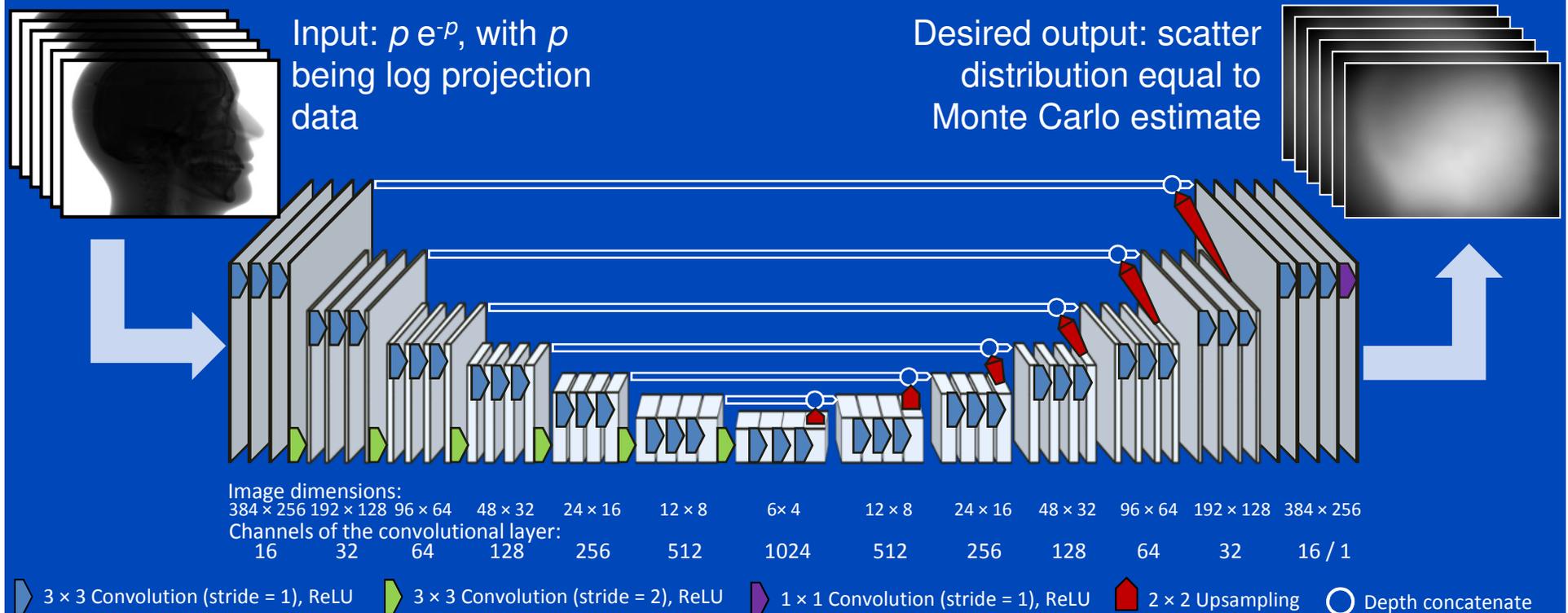
**1 to 10 hours  
per tomographic data set**



# Deep Scatter Estimation<sup>1,2</sup> (DSE)

## Basic Principle

- Optimize weights and biases of convolutional network such that the error between the output and a MC scatter simulations is minimal.

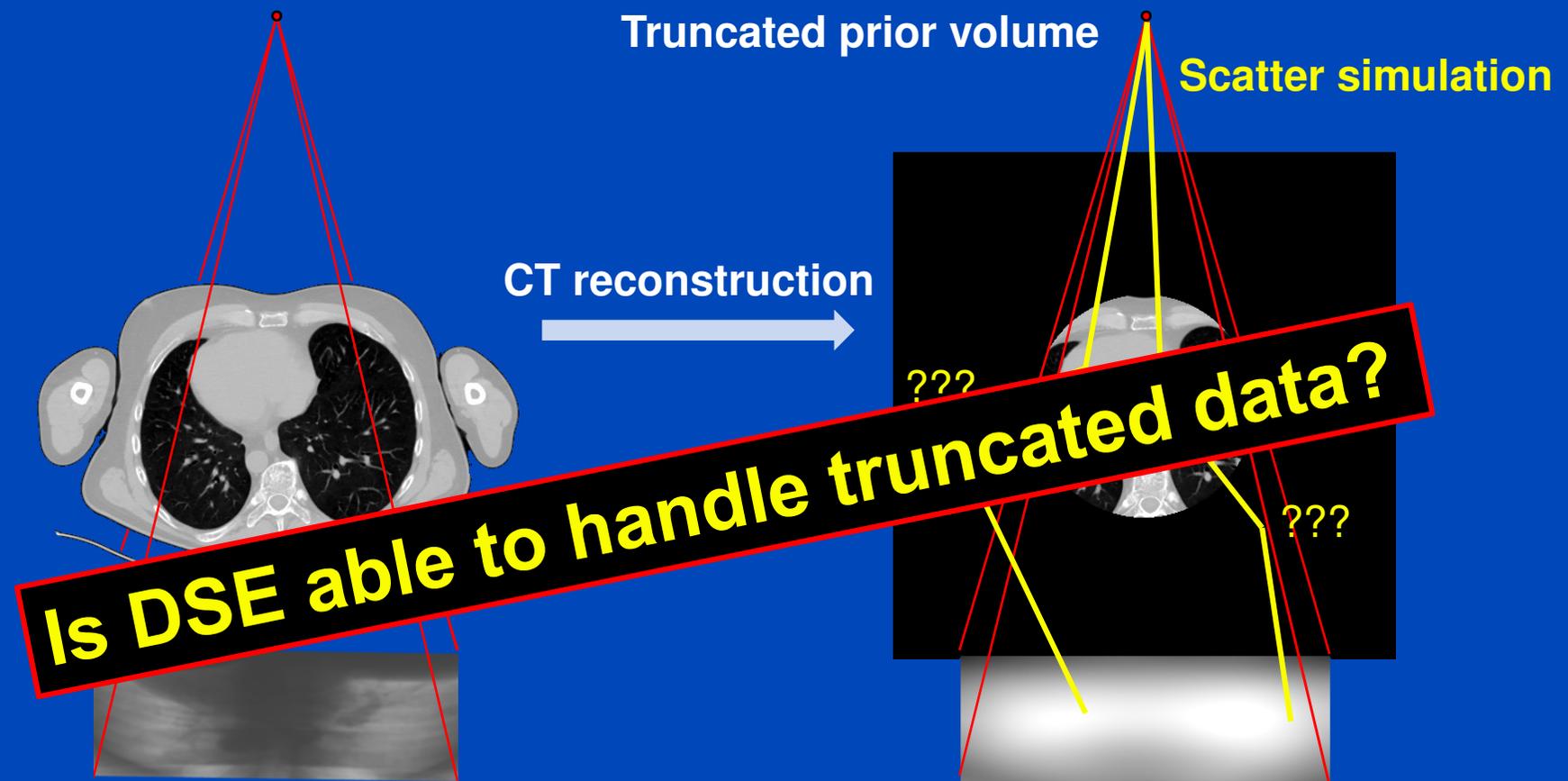


<sup>1</sup>J. Maier, Y. Berker, S. Sawall, M. Kachelrieß. SPIE Medical Imaging Conference Record 105731L:1-6, 2018.

<sup>2</sup>J. Maier, S. Sawall, M. Knaup, M. Kachelrieß. Journal of Nondestructive Evaluation 37:57, 2018.

# Data Truncation

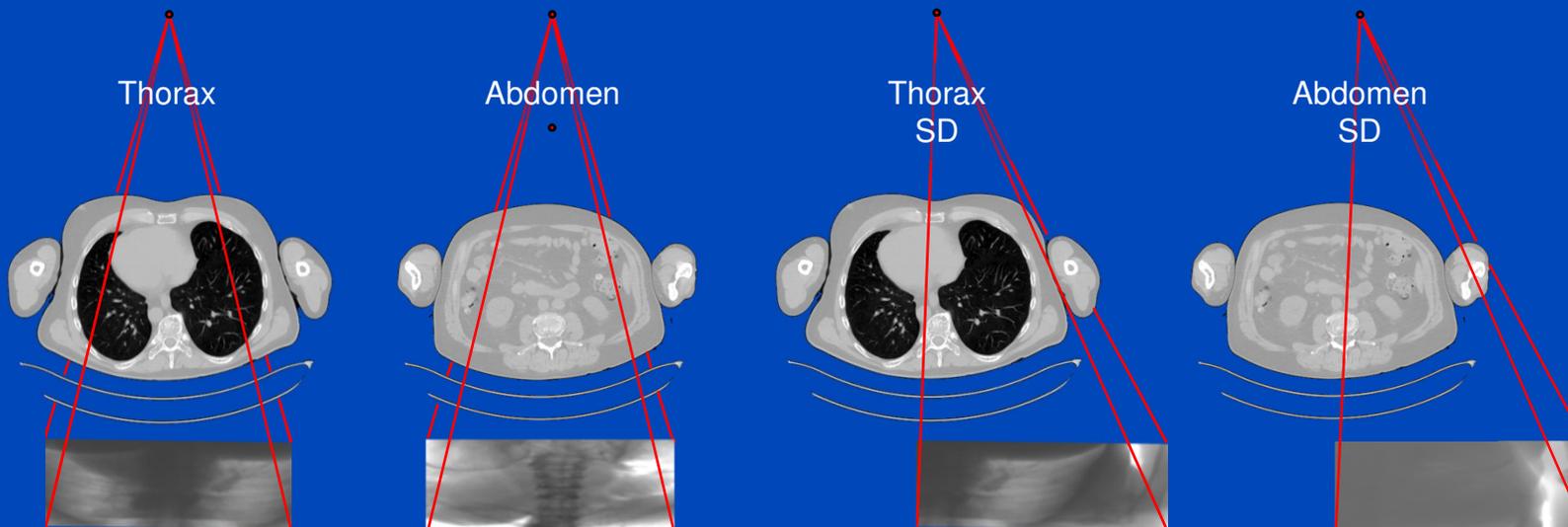
- CBCT often has to deal with truncation which.
- Truncation decreases the performance of scatter estimation approaches such as MC or Boltzmann transport<sup>1</sup>.



<sup>1</sup>N. Waltrich, D. Sawall, J. Maier, J. Kuntz, K. Stannigel, K. Lindenberg, and M. Kachelrieß. Effect of detruncation on the accuracy of Monte Carlo-based scatter estimation in truncated CBCT. Med. Phys. 45(8):3574–3590, 2018.

# Simulation Study

- Simulation of head, thorax and abdomen CBCT data using 14 clinical CT patient data sets as a starting point.
- Typical CBCT geometry and a 40 × 30 cm flat detector.
- Two different setups:
  - centered detector
  - shifted detector (SD)
- Simulation of scatter using our in house MC simulation<sup>1</sup>.



<sup>1</sup>M. Baer, M. Kachelrieß: Hybrid scatter correction for CT imaging. Phys. Med. Biol. 57: 6849–6867, 2012.

# DSE Training & Testing

- Simulation of 30240 head, thorax and abdomen projections.
- Splitting into 80% training data and 20% test data.
- The DSE network was trained to learn the mapping:

$$M_{\text{pep}} : p \cdot e^{-p} \rightarrow S_{\text{MC}}$$

- The weights  $w$  and the biases  $b$  were determined by minimizing the mean absolute percentage error between the output and a MC scatter prediction  $S_{\text{MC}}$ :

$$\{w, b\} = \operatorname{argmin} \frac{100}{K} \sum_{n, u} \left| \frac{\text{DSE}(n, u, w, b) - S_{\text{MC}}(n, u)}{S_{\text{MC}}(n, u)} \right|$$

- The training was performed on an NVIDIA Quadro P6000 for 80 epochs using an Adam optimizer and a batch size of 16.
- Training took about 15 h.
- Training on each anatomy separately or using all data together.

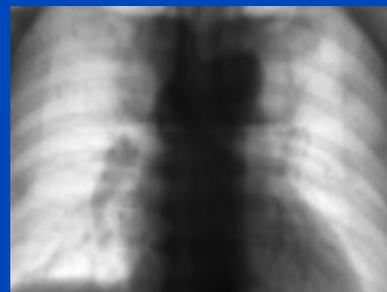
# Kernel-based Scatter Estimation (KSE)

## (Reference 1)

- Kernel-based scatter estimation<sup>1</sup>:

- Estimation of scatter by a convolution of the scatter source term  $T(p)$  with a scatter propagation kernel  $G(\mathbf{u}, \mathbf{c})$ :

$$I_{s, \text{est}}(\mathbf{u}) = \underbrace{\left( c_0 \cdot p(\mathbf{u}) \cdot e^{-p(\mathbf{u})} \right)}_{T(p)(\mathbf{u})} * \underbrace{\left( \sum_{\pm} e^{-c_1(\mathbf{u}\hat{\mathbf{e}}_1 \pm c_2)^2} \cdot \sum_{\pm} e^{-c_3(\mathbf{u}\hat{\mathbf{e}}_2 \pm c_4)^2} \right)}_{G(\mathbf{u}, \mathbf{c})}$$



$T(p)(\mathbf{u})$

Open parameters:  
 $c_0$



$G(\mathbf{u}, \mathbf{c})$

Open parameters:  
 $c_1, c_2, c_3, c_4$

$$\{c_i\} = \operatorname{argmin} \sum_n \sum_{\mathbf{u}} \|I_{s, \text{est}}(n, \mathbf{u}, \{c_i\}) - I_s(n, \mathbf{u})\|_2^2,$$

Samples of the training data set

Detector coordinate

Scatter estimate



MC scatter simulation



<sup>1</sup>B. Ohnesorge, T. Flohr, K. Klingenberg-Regn: Efficient object scatter correction algorithm for third and fourth generation CT scanners. Eur. Rad. 9:563–569, 1999.

# Hybrid Scatter Estimation (HSE) (Reference 2)

- Hybrid scatter estimation<sup>1</sup>:

- Estimation of scatter by a convolution of the scatter source term  $T(p)$  with a scatter propagation kernel  $G(\mathbf{u}, \mathbf{c})$ :

$$I_{s, \text{est}}(\mathbf{u}) = \underbrace{\left( c_0 \cdot p(\mathbf{u}) \cdot e^{-p(\mathbf{u})} \right)}_{T(p)(\mathbf{u})} * \underbrace{\left( \sum_{\pm} e^{-c_1(\mathbf{u}\hat{\mathbf{e}}_1 \pm c_2)^2} \cdot \sum_{\pm} e^{-c_3(\mathbf{u}\hat{\mathbf{e}}_2 \pm c_4)^2} \right)}_{G(\mathbf{u}, \mathbf{c})}$$



$T(p)(\mathbf{u})$   
Open  
parameters:  
 $c_0$



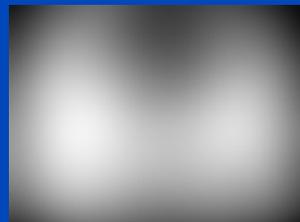
$G(\mathbf{u}, \mathbf{c})$   
Open  
parameters:  
 $c_1, c_2, c_3, c_4$

$$\{c_i\}_n = \operatorname{argmin} \sum_{\mathbf{u}} \|I_{s, \text{est}}(n, \mathbf{u}, \{c_i\}) - I_s(n, \mathbf{u})\|_2^2,$$

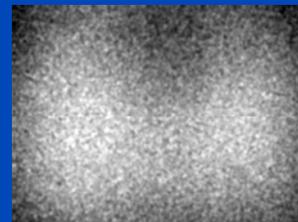
Samples of the test  
data set

Detector  
coordinate

Scatter estimate



Coarse MC scatter simulation



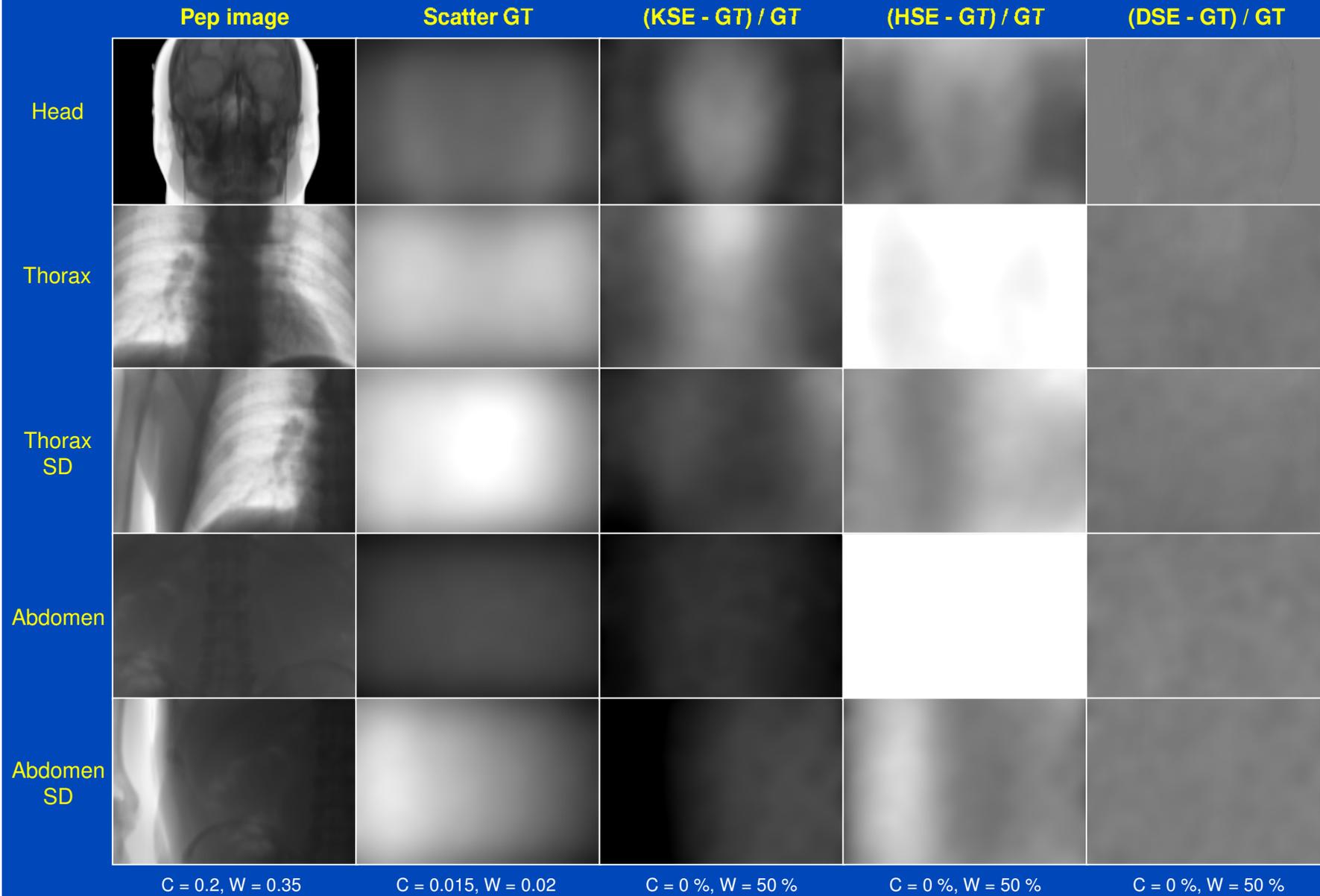
# Results

<b>KSE</b>	Head	Thorax	Abdomen
Head	<b>14.5</b>	26.8	32.5
Thorax	16.2	<b>18.5</b>	19.4
Abdomen	16.8	22.1	<b>17.8</b>
All data	<b>14.9</b>	<b>20.5</b>	<b>19.3</b>

<b>DSE</b>	Head	Thorax	Abdomen
Head	<b>1.2</b>	21.1	32.7
Thorax	8.8	<b>1.5</b>	9.1
Abdomen	11.9	10.9	<b>1.3</b>
All data	<b>1.8</b>	<b>1.4</b>	<b>1.4</b>

Values shown are the mean absolute percentage errors (MAPEs) of the testing data.

# Scatter Estimates



Ground truth

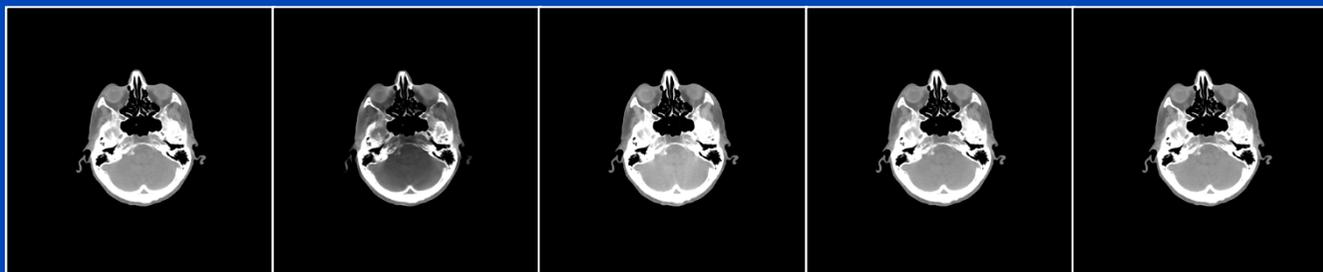
No correction

KSE

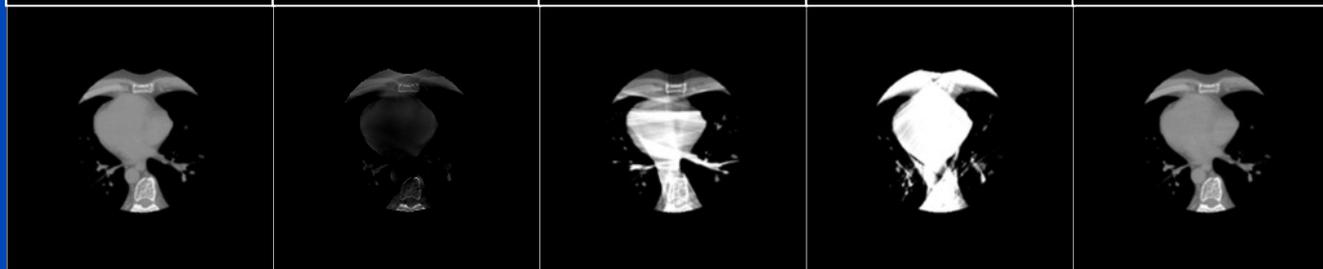
HSE

DSE

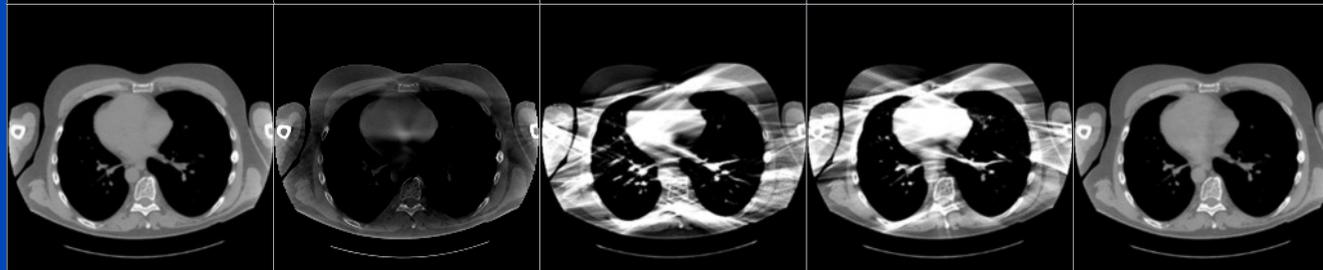
Head  
22 cm FOM



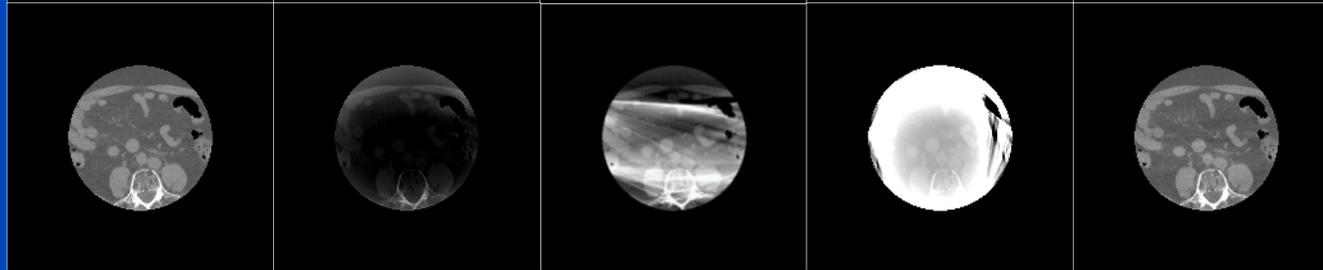
Thorax  
22 cm FOM



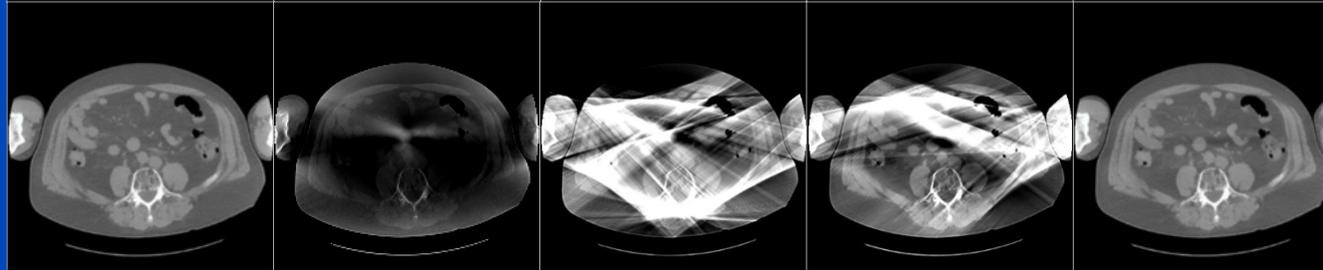
Thorax  
SD  
40 cm FOM



Abdomen  
22 cm FOM



Abdomen  
SD  
40 cm FOM



140 kV  
C = 0 HU, W = 700 HU

Ground truth

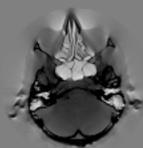
No correction

KSE

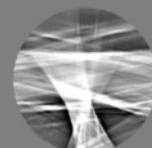
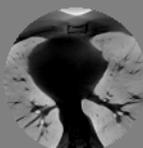
HSE

DSE

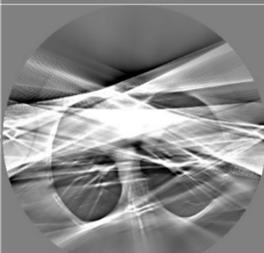
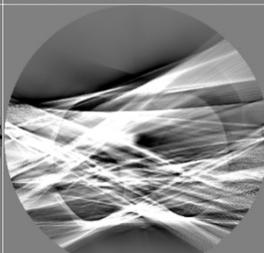
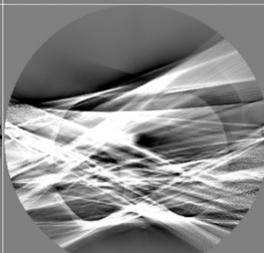
Head  
22 cm FOM



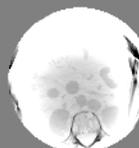
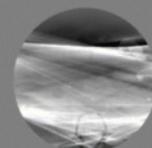
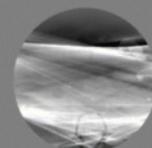
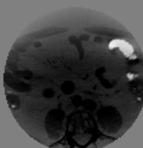
Thorax  
22 cm FOM



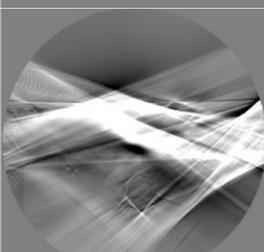
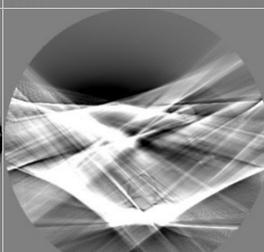
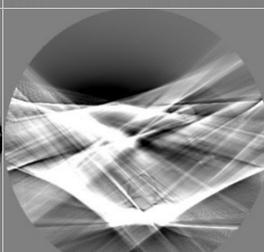
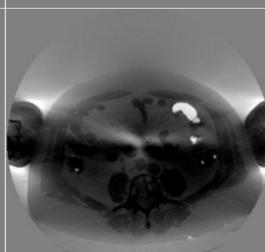
Thorax  
SD  
40 cm FOM



Abdomen  
22 cm FOM



Abdomen  
SD  
40 cm FOM



Difference to GT  
C = 0 HU, W = 700 HU

# Conclusions

- DSE yields scatter estimates that only differ by about 1.5% on average from the ground truth.
- DSE outperforms conventional kernel-based approaches in terms of accuracy and speed (DSE = 10 ms/projection)
- DSE generalizes well to varying anatomical regions. A single DSE network can correct for head, thorax and abdomen data.
- Interesting observations
  - DSE can estimate scatter from a single (!) x-ray image.
  - DSE can accurately estimate scatter from a primary+scatter image, but
  - DSE cannot accurately estimate scatter from a primary only image.
  - DSE may outperform MC even though DSE is trained with MC.
- DSE is not restricted to reproducing MC scatter estimates. It can obviously be used with any other scatter estimate.

# Thank You!



## The 6<sup>th</sup> International Conference on Image Formation in X-Ray Computed Tomography

August 3 - August 7 • 2020 • Regensburg • Germany • [www.ct-meeting.org](http://www.ct-meeting.org)



© Bild Regensburg Tourismus GmbH

Conference Chair: **Marc Kachelrieß**, German Cancer Research Center (DKFZ), Heidelberg, Germany

This presentation will soon be available at [www.dkfz.de/ct](http://www.dkfz.de/ct).  
Job opportunities through DKFZ's international Fellowship programs ([marc.kachelriess@dkfz.de](mailto:marc.kachelriess@dkfz.de)).  
Parts of the reconstruction software were provided by RayConStruct® GmbH, Nürnberg, Germany.